Introduction to Complex Analysis (Engineers), 201.1.0071, BGU Spring 2017

Lectures: Dmitry Kerner, (Sundays 9:00-10:00, Thursdays 18:00-20:00).

Office hours ([58], room 217, kernerdm@math.bgu.ac.il): https://www.math.bgu.ac.il/en/teaching/hours The site of the course: $https: //www.math.bgu.ac.il/ \sim kernerdm$

<u>Tutorials</u>: Yonatan Yehezkeally (Sundays 16:00-17:00, Tuesdays 18:00-19:00, 19:00-20:00).

The structure of the final grade

There will be about 10-12 homeworks. There will be one midterm (date: ??). The final mark is computed as: $10\%(midterm) + 90\%(final\ exam)$. The final exams are: Moed A (20.07.2017), Moed B (10.08.2017).

The textbooks:

- Ahlfors, Complex analysis.
- Nehari, Conformal mapping.
- J.Bak, D.J.Newman, Complex Analysis.
- D, Alpay, A Complex Analysis problem book.

The program of the course (the order of the topics is approximate and will be adjusted during the semester)

- (1) Complex numbers, open and closed sets in \mathbb{C} , (path) connectedness. The extended complex plane (Riemann sphere), $\overline{\mathbb{C}}$. e^z and De Moivre formula.
- (2) Functions of a complex variable, continuity and real-differentiability. Complex-differentiability and Cauchy-Riemann equations. Functions holomorphic in a domain. Basic properties of the complex derivative.
- (3) Power series. Review of convergence of functions, uniform convergence on compacts. Radius of convergence of a power series. Differentiation of power series. Analytic functions. Taylor series for e^z, sin(z), cos(z).
- (4) Curvilinear (complex) integrals. The Cauchy-Goursat theorem. The Cauchy integral formula. Morera's theorem.

Uniform convergence of holomorphic functions on a compact set. The maximum principle. Liouville's theorem. The Laplace transform as a holomorphic function on a half-plane.

- (5) Laurent series. Annulus of convergence, existence of Laurent series expansions.
- (6) Zeroes and singularities. Order of a zero and a pole. Classification of singularities. Principal singularities, the Casorati-Weierstrass theorem. The Riemann sphere and a meromorphic function. The residue theorem. Computations of integrals.
- (7) The Argument Principle. The maximum principle. Rouché's theorem. The open mapping theorem. Hurewicz's theorem.
- (8) Harmonic functions. The harmonic conjugate. The average and maximum principles for harmonic functions. Finding harmonic functions satisfying boundary conditions (e.g. on a strip).
- (9) Conformal maps. Branches of log. Schwarz' lemma.
- (10) Stereographic projection.

Möbius transformations. Criteria for fixing the unit disk and the upper half plane. Statement of the Riemann mapping theorem. Examples of conformal maps.

Schwarz-Christoffel transformations. Applications to harmonic functions (electrostatic potential with boundary conditions). The punctured disk is not conformally equivalent to an annulus.