

Department of Mathematics, BGU

---

---

BGU Probability and Ergodic Theory  
(PET) seminar

---

---

*On Thursday, November ,10 2022*

*At 11:10 – 12:00*

**In 101-**

Jean-Pierre Conze (French National Centre for Scientific Research)

will talk about

**Sampling a random field along a stationary  
process, related questions in ergodic theory**

Abstract:

Title: Sampling a random field along a stationary process, related questions in ergodic theory

## Abstract

For a sequence  $(X_k)$  of real iid random variables with common probability distribution function  $F$ , the empirical process is defined by  $W_n(s) := \sum_{k=0}^{n-1} [\mathbf{1}_{X_k \leq s} - F(s)]$ .

Among classical results on this process, the following are well known.

- the Glivenko-Cantelli theorem:  $\sup_s \frac{1}{n} |W_n(s)| \rightarrow 0$ ;
- a functional central limit theorem for  $W_n(s)$  after normalisation.

We will present extensions of these results when the process is sampled along a sequence of times  $(z_n)$ , in particular when  $(z_n)$  is a sequence of ergodic sums generated by a dynamical system.

More precisely, if  $(X, \mu, T)$  is a dynamical system and  $f : X \rightarrow \mathbb{Z}^d$ , we take, for  $x \in X$ ,  $z_n = S_n(x) := \sum_{k=0}^{n-1} f(T^k x)$ ,  $n \geq 1$ . Then, if  $(X_{\underline{\ell}}, \underline{\ell} \in \mathbb{Z}^d)$  is a random field indexed by  $\mathbb{Z}^d$  of real iid r.v.s (or more generally of associated r.v.s), we study the sampled process  $(X_{S_n(x)})_{n \geq 1}$ .

To apply general criteria, a precise information about the number of visits of  $S_n$  to a site before time  $n$  is needed. We will give examples where we can conclude. When  $(S_n)$  is a random walk, this is related to limit theorems in random scenery and to results (going back to Erdős and several authors) on limit laws for the “maximal multiplicity” in  $n$  steps of a random walk.

This is a joint work with Guy Cohen (Ben-Gurion University).