The Department of Mathematics
2019–20–B term

Course Name  Field Theory and Galois Theory
Course Number 201.1.7041


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Office Hours  https://www.math.bgu.ac.il/en/teaching/hours

Abstract

Requirements and grading

Course topics

• Fields: basic properties and examples, the characteristic, prime fields
• Polynomials: irreducibility, the Eisenstein criterion, Gauss’s lemma
• Extensions of fields: the tower property, algebraic and transcendental extensions, adjoining an element to a field
• Ruler and compass constructions
• Algebraic closures: existence and uniqueness
• Splitting fields
• Galois extensions: automorphisms, normality, separability, fixed fields, Galois groups, the fundamental theorem of Galois theory.

Information may change during the first two weeks of the term. Please consult the webpage for updates
- Cyclic extensions

- Solving polynomial equations by radicals: the Galois group of a polynomial, the discriminant, the Cardano-Tartaglia method, solvable groups, Galois theorem

- Roots of unity: cyclotomic fields, the cyclotomic polynomials and their irreducibility

- Finite fields: existence and uniqueness, Galois groups over finite fields, primitive elements