The Sixth Israeli Mini-Workshop in Applied Mathematics Dedicated to the Memory of Lee Segel (1932-2005)

Sponsored by: ***CENTER FOR ADVANCED STUDIES IN MATHEMATICS (BGU)***

Organizers: Vladimir Gol'dshtein and Boris Zaltzman

We are pleased to invite the Israeli applied math. community to participate in the Sixth Israeli Mini-Workshop in Applied and Computational Mathematics, to be held at the Ben-Gurion University on Monday January 1st, 2007.

The idea of the workshop is to create a forum for researchers in applied mathematics, especially younger faculty and students, to get to know each other, and promote discussion and collaboration between researchers from various disciplines and institutions. The workshop will take place in Ben-Gurion University, Mathematical Department (building 58), room -101. See Campus Map at http://www.cs.bgu.ac.il/information/directions.html.

We dedicate this mini-workshop to the memory of Lee Segel (February 5, 1932 – January 31, 2005), a great scientist, a wonderful man, one of the leading applied mathematicians and a pioneer of Modern Mathematical Biology.

To register, please send a short e-mail to the organizers at boris@bgu.ac.il. There is no registration fee, but we need to know how many participants to expect.

The tentative schedule:

Registration: 9.30 till 12.15

10:30	Isaak Rubinstein (Ben-Gurion University)	Opening and Tribute to Lee Segel (1932-2005)
10:45 - 11:15	Baruch Meerson (Hebrew University)	Spectral theory of metastability and extinction in birth-death systems
11:15 - 11:45	Moshe Goldberg (Technion)	Stable finite-difference approximation for parabolic systems
11:45 - 12:20	Coffee break	
12:20 - 12:50	Leonid Berezansky (Ben-Gurion University)	Delay differential equations of mathematical biology

12:45 - 14:20	Lunch break	
14:20 - 14:50	Len Pismen (Technion)	Wandering patterns in reactive dewetting
14:50 - 15:20	Gadi Fibich (Tel-Aviv University)	New singular solutions of the nonlinear Shrodinger equation
15:20 - 15:50	Daniel Michelson (Weizmann Institute)	Radial asymptotically periodic solutions of the Kuramoto-Sivashinsky equation
15:50 - 16:20	Coffee break	
16:20 - 16:50	Isaac Goldhirsch (Tel-Aviv University)	Strongly inelastic granular gases
16:50 - 17:20	Itzhak Fouxon (Hebrew University)	Formation and evolution of particle clusters in inelastic gases
17:20 - 17:50	Ehud Yariv (Technion)	Electro-magneto-phoresis of slender bodies

Abstracts:

Spectral theory of metastability and extinction in birth-death systems

Baruch Meerson (Hebrew University)

Statistics of rare events (or large deviations) in birth-death systems have attracted a great deal of interest in many areas of science including physics, chemistry, astrochemistry, epidemiology, population biology, cell biochemistry *etc.* We suggest a general spectral method [1,2] for calculating statistics of (not necessarily single-step) birth-death processes and chemical reactions which possess an absorbing state. The method employs the generating-function formalism in conjunction with the Sturm-Liouville theory of linear differential operators. It yields accurate results for the extinction statistics and for the quasi-stationary probability distributions, including large deviations, of metastable states. The power of the method is demonstrated on the example of branching and annihilation $A \to 2A$, $2A \to \emptyset$, representative of a rather general class of processes.

References

[1] M. Assaf and B. Meerson, Phys. Rev. Lett. **97**, 200602 (2006).

[2] M. Assaf and B. Meerson, cond-mat/0612157.

Stable Finite-Difference Approximations for Parabolic Systems

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ABSTRACT. In this talk we discuss stability criteria for a family of finite-difference approximations to parabolic initial-value problems of the form

$$\frac{\partial \mathbf{u}(x,t)}{\partial t} = \sum_{1\le p\le q\le s} A_{pq} \frac{\partial^2 \mathbf{u}(x,t)}{\partial x_p \partial x_q} + \sum_{1\le p\le s} B_p \frac{\partial \mathbf{u}(x,t)}{\partial x_p} + C\mathbf{u}(x,t),$$

$$\mathbf{u}(x,0) \in L_2, \quad x = (x_1,\ldots,x_s) \in \mathbb{R}^s, \quad 0 \le t \le T,$$

where A_{pq}, B_p, and C are constant matrices. We deal with two cases, the classical case where the leading matrix coefficients A_{pq} are Hermitian, and the less conventional case where the A_{pq} are triangular. The second case arise in connection with a number of physical and biological applications; for instance, heat and mass transfer with Soret and Dufour cross-effects, segregation dynamics of granular materials, and interacting population dynamics with dispersion. This is joint work with Anna Pidgirnyak.

Delay differential equations of mathematical biology

Leonid Berezansky (Ben-Gurion University)

I will review the results of our study of the delay differential equation models in mathematical biology (e.g., Logistic equation with harvesting; Hematopoiesis equation; Food-limited equation; Periodic Fox production equation) and address questions of solution oscillation, local and global stability, existence of periodic solutions, extinction and persistence.

Wandering patterns in reactive dewetting

Len Pismen (Technion)

A change of wetting properties of a liquid as a result of a chemical reaction, phase transition or thermal flux, may cause self-propelled motion of droplets observed in a number of experiments. The velocity of motion can be computed analytically using integral conditions that involve both boundary forcing and viscous friction (resolving the latter's singularity at the contact line). Repelling interaction of droplets may lead, depending on the ratio of motion and diffusion times, to mutual scattering or pattern formation, reproducing in a peculiar form related phenomena in activator-inhibitor systems.

New singular solutions of the nonlinear Shrodinger equation

Gadi Fibich (Tel-Aviv University)

The study of singular solutions of the NLS goes back to the 1960s, with applications in nonlinear optics and, more recently, in BEC. Until recently, the only known singular solutions had a self-similar “Gaussian-type” profile that approaches a delta function near the singularity. In this talk I will present new families of singular solutions of the NLS that collapse with a self-similar ring profile, and whose blowup rate is different from the one of the “old” singular solutions. I will also show, both theoretically and experimentally, that these new blowup profiles are attractors for large super-Gaussian initial conditions.

Radial asymptotically periodic solutions of the Kuramoto-Sivashinsky equation

Daniel Michelson (Weizmann Institute)

Rotationally invariant steady solutions of the Kuramoto-Sivashinsky equation in the two space dimensions are studied. It is shown that there exist solutions that approach at infinity the one-dimensional periodic solutions. Both hyperbolic and elliptic periodic solutions are considered.

Strongly inelastic granular gases

Isaac Goldhirsch (Tel-Aviv University)

A novel method for analyzing the Boltzmann equation corresponding to inelastically colliding particles ("grains") has been developed. It is

based on several elements, including the observation that the Sonine polynomial expansion for the homogeneous cooling state is asymptotic (though Borel resumable) and the fact that high order expansions in these polynomials may be conveniently carried out by employing the power of symbolic manipulators (such as MAPLE). The results for the transport coefficients are in excellent agreement with DSMC simulations (unlike all previous results) for all physical values of the coefficient of normal restitution. Further applications and implications will be discussed, time allowing.

Formation and evolution of particle clusters in inelastic gases

Itzhak Fouxon (Hebrew University)

Among the phenomena of structure formation in many-body systems, one of the most interesting is development of clusters of matter from structureless initial states. A most familiar example is gravitational instability, important for the structure formation in the Universe. Another example is clustering instability of a dilute gas of inelastically colliding particles. Such a gas, left alone, behaves opposite to the usual gas – instead of spreading uniformly over the container, it forms regions of high density. Both instabilities are hard to describe beyond the linear theory due to the absence of the regime of weak non-linearity. In this talk we consider the clustering instability in the case of a narrow channel geometry of the container, which confines the gas dynamics to a single spatial dimension. We derive analytic solutions of the fully non-linear system of gas dynamic equations and show that they produce, in a finite time, a new type of hydrodynamic singularity – density spikes. The singularity holds universally for generic initial conditions, and it signals formation of a new phase, where gas particles are densely packed. We continue the solutions beyond the singularity (weak solutions) where they describe a gas flow for which the dilute and the dense phases coexist. The mass of the densely packed regions grows with time. Development of such growing particle clusters can be important for the formation of planet-like bodies in the Universe.

Electro-magneto-phoresis of slender bodies

Ehud Yariv (Technion)

When an insulating particle is placed within a conducting liquid domain which is exposed to uniformly-applied electric and magnetic fields, a rotational Lorentz force density distribution is generated, thereby animating liquid flow. The consequent particle motion is known as Electro-magneto-phoresis (EMP). This mechanism, traditionally employed for impurity extraction in liquid metals, now finds new applications for the manipulation, control and separation of bio- particles.

Symmetry analyses have already demonstrated that the combination of electric and magnetic fields can result in a rich topology of particle motion, unparalleled by other (e.g. phoretic) animation mechanisms. So far, however, analytic solutions for EMP have only been obtained for highly-symmetric particle shapes (spheres and ellipsoids) which

do not exhibit the entire richness of particle motions. In this talk, I will describe how slender-body asymptotic theory can be exploited to analyze the EMP of elongated particles which are arbitrarily oriented relative to the externally-imposed fields.

Joint work with Touvia Miloh, Tel Aviv University