

Department of Mathematics, BGU

Operator Algebras and Operator Theory

On Monday, December 4, 2017

At 16:00 – 17:00

In 101-

Gregory Marx (BGU)

will talk about

Completely Positive Noncommutative Kernels, part 2

Abstract: It is well known that a function $K : \Omega \times \Omega \rightarrow \mathcal{L}(\mathcal{Y})$ (where $\mathcal{L}(\mathcal{Y})$ is the set of all bounded linear operators on a Hilbert space \mathcal{Y}) being (1) a positive kernel in the sense of Aronszajn (i.e. $\sum_{i,j=1}^N \langle K(\omega_i, \omega_j) y_j, y_i \rangle \geq 0$ for all $\omega_1, \dots, \omega_N \in \Omega$, $y_1, \dots, y_N \in \mathcal{Y}$, and $N = 1, 2, \dots$) is equivalent to (2) K being the reproducing kernel for a reproducing kernel Hilbert space $\mathcal{H}(K)$, and (3) K having a Kolmogorov decomposition $K(\omega, \zeta) = H(\omega)H(\zeta)^*$ for an operator-valued function $H : \Omega \rightarrow \mathcal{L}(\mathcal{X}, \mathcal{Y})$ where \mathcal{X} is an auxiliary Hilbert space.

Last time, I introduced free noncommutative function theory and wrote down the analogue of the result above for noncommutative kernels. In part two, I will give a sketch of our proof and discuss some well-known results (e.g. Stinespring's dilation theorem for completely positive maps) which follow as corollaries. With any remaining time, I will talk about applications and more recent related results.