## Department of Mathematics, BGU

## **AGNT**

On Tuesday, November, 8 2022

At 12:40 - 13:40

In 201

Yotam Hendel (Université de Lille)

will talk about

## On unflorm number theoretic estimates for fibers of polynomial maps over finite rings of the form $Z/p^{\wedge}kZ$

Abstract: Let  $f:X \to Y$  be a morphism between smooth, geometrically irreducible Z-schemes of finite type. We study the number of solutions  $\#\{x:f(x)=y \mod p^k\}$  for prime p, positive number k, and  $y \in Y(Z/p^kZ)$ , and show that the geometry and singularities of the fibers of f determine the asymptotic behavior of this quantity as p, k and y vary.

In particular, we show that f:X \to Y is flat with fibers of rational singularities, a property abbreviated (FRS), fi and only fi  $\#\{x:f(x)=y \mod p^k\}/p^{k(\dim X - \dim Y)\}$  is unfiormly bounded in p, k and y. We then consider a natural family of singularity properties, which are variants of the (FRS) property, and provide for each member of this family a number theoretic characterization using the asymptotics of  $\#\{x:f(x)=y \mod p^k\}/p^{k(\dim X - \dim Y)\}$ .

To prove our results, we use model theoretic tools (and in particular the theory of motivic integration, in the sense of unflorm p-adic integration) to effectively study the collection  $\{\#\{x:f(x)=y \mod p^k\}/p^k(\dim X -\dim Y)\}$ . If time allows, we will discuss these methods.

Based on a joint work with Raf Cluckers and Itay Glazer.

Please Note the Unusual Place!