

Department of Mathematics, BGU

BGU Probability and Ergodic Theory (PET) seminar

On *Thursday, February 22, 2024*

At *11:10 – 12:00*

In *101-*

Michael Lin (BGU)

will talk about

Uniform ergodicity and the one-sided ergodic Hilbert transform

Abstract: Let T be a bounded linear operator on a Banach space X satisfying $\|T^n\| \rightarrow 0$. We prove that T is uniformly ergodic if and only if the one-sided ergodic Hilbert transform $H(T)x := \lim_{n \rightarrow \infty} \sum_{k=1}^n k^{-1} T^k x$ converges for every $x \in \overline{(I-T)X}$. When T is a power-bounded (or more generally (C, α) -bounded for some $0 < \alpha < 1$), then T is uniformly ergodic if and only if the domain of H equals $(I-T)X$.