

המחלקה למתמטיקה

סמסטר 20-2019-ב

שם הקורס אלגברה הומוטופית

מספר קורס 201.2.2091

עמוד הקורס ברשת

https://www.math.bgu.ac.il/~amyekut/teaching/2019-20/homol-alg/course_page.html

מרצה אחראי פרופ' אמנון יקותיאלי, <amyekut@bgu.ac.il>, חדר 202

שעות קבלה <https://www.math.bgu.ac.il/he/teaching/hours>

תקציר

Description: This course is for undergraduate students. The prerequisite is Algebra I. The course covers: free functors; exact and additive functors; and categories of rings and modules of products tensor coproducts; determined by the course, the amount of material covered, the pace of the course, the background and capability of the audience. There will be many examples and lectures. I will upload typed notes after every lecture. Exercises will be assigned and submitted. *Grade:* Course grade is determined by the most homework submitted and checked every week. *Homework:* To be assigned every week. *See* administrative information for handout day first.

Topics: Course

1. Adjoint functors.

2. Morita Theory.

3. Injective and Projective modules.

4. Complexes of modules.

5. Homotopies and homotopy equivalences.

- .6 The long exact cohomology sequence.
- .7 Projective, flat and injective resolutions.
- .8 Left and right derived functors.
- .9 Applications of derived functors to commutative algebra.
- .10 Further applications of derived functors and cohomology.

דרישות והרכב ציון הקורס¹

¹דרישות הקורס יכולות להשתנות במהלך השבועיים הראשונים של הסמסטר, ויש לשים לב להודעות באתר הקורס



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פרופ' אמנון יקותיאל
המחלקה למתמטיקה
אוניברסיטת בן גוריון
באר שבע 84105

22 February 2020

Course Announcement:
Homological Algebra
Spring Semester 2019-20

Catalog Number: 201.2.2091

Time: Wednesday 12:00 – 14:00

Place: Building 58 room 201

First meeting: 11 March 2020

Teaching Language: English

Web Page: https://www.math.bgu.ac.il/~amyekut/teaching/2019-20/homol-alg/course_page.html

Description: This is a graduate level course. Undergraduate students can register with my permission.

The prerequisite course is "Commutative Algebra" that I gave in the fall semester (or an equivalent course). We will need the following topics from that course: categories and functors; additive and exact functors; free modules; products and coproducts; tensor products of modules and rings.

The pace of the course, and the amount of material covered, will be determined by the background and capability of the audience. There will be many examples and exercises. I will upload typed notes after every lecture.

Course Grade: pass/fail grade. Passing the course requires attending all lectures and submitting most of the homework.

Homework: To be assigned every week. Checking will be sporadic.

See the first day handout for more administrative information.

Course Topics:

1. Adjoint functors.
2. Morita Theory.
3. Projective and Injective modules.
4. Complexes of modules.
5. Homotopies and homotopy equivalences.
6. The long exact cohomology sequence.
7. Projective, flat and injective resolutions.
8. Left and right derived functors.
9. Applications of derived functors to commutative algebra.
10. Further applications of derived functors and cohomology.

Bibliography:

1. P.J. Hilton and U. Stammbach, "A Course in Homological Algebra", Springer, 1971.
2. S. MacLane, "Homology", Springer, 1994.
3. J. Rotman, "An Introduction to Homological Algebra", Academic Press, 1979.
4. L.R. Rowen, "Ring Theory" (Student Edition), Academic Press, 1991.
5. C. Weibel, "An introduction to homological algebra", Cambridge Univ. Press, 1994.
6. A. Yekutieli, "Derived Categories", Cambridge Univ. Press, 2019.
7. Course notes, to be uploaded every week to the [course web page](#).

נושאי לימוד

- .1 modules ideals, noncommutative), (including Rings material. prior Recalling tensor products, and sums direct infinite sequences, exact bimodules, and rings. and modules of products
- .2 categories Linear equivalences. functors, of Morphisms functors. and Categories functors. of Exactness functors. linear and
- .3 modules. flat and injective Projective, modules. Special
- .4 products. tensor as realized categories module of Equivalences Theory. Morita
- .5 long the homotopies, complexes, on Operations modules. of Complexes sequence. cohomology exact
- .6 uniqueness. and existence – resolutions flat and injective Projective, Resolutions.
- .7 functors. Ext and Tor theory. general The functors. derived right and Left
- .8 involving theorems, global and local Some algebra. commutative to Applications functors. torsion and completion Derived functors. *Ext* and *Tor*
- .9 geometry. in algebra homological of role the of survey A cohomology. Sheaf
- .10 cohomology, Galois theorems: classification of survey A cohomology. Nonabelian bundles. vector

Bibliography

- .1977 New-York, Springer-Verlag, Geometry”, “Algebraic Hartshorne, R. .1
- Springer, Algebra”, Homological in Course “A Stammbach, U. and Hilton P.J. .2
.1971
- .1994 Springer, “Homology”, Maclane, S. .3
- .1979 Press, Academic Algebra”, Homological to Introduction “An Rotman, J. .4
- .1991 Press, Academic Edition), (Student Theory” “Ring Rowen, L.R. .5
- Press, Univ. Cambridge algebra”, homological to introduction “An Weibel, C. .6
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- .1990 Springer, Manifolds, on Sheaves Schapira, P. and Kashiwara M. .7

Yekutieli, A. (9) (Editor). Jong de J.A. reference, online an,²Project Stacks The .8
prepublication Free .2019 Press, Univ. Cambridge Categories”, “Derived
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²<http://stacks.math.columbia.edu>

³<https://arxiv.org/abs/1610.09640v4>