

$$f_x = \frac{(x+h)^2 \cdot 0 - x^2 \cdot 0}{h} = \frac{0 - 0}{h} = 0$$

~~$f_x = \frac{x^2 \cdot (y+h) - x^2 \cdot y}{h}$~~

$$f_x = \frac{(x+h)^2 \cdot 0 - x^2 \cdot 0}{(x+h)^{10} + y^2} = \frac{0 - 0}{x^{10} + y^2} = 0$$

$$\frac{h^2 \cdot 0}{h^2} = \frac{0}{h^2} = 0$$

~~for the second part~~

$$f_y = \frac{x^2 \cdot (y+h) - x^2 \cdot y}{(x+h)^{10} + (y+h)^2} = \frac{x^2 \cdot h}{x^{10} + y^2 + 2yh + h^2} = 0$$

$$\lim_{h \rightarrow 0} \frac{f(x, y+h) - f(x, y)}{h} = 0$$

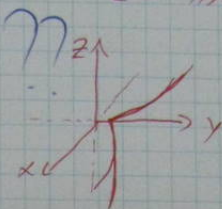
←
QED

5

$$-3x^2 + 5y^2 + 7z^2 - 1 = 0$$

z=0 קריטר

$$-3x^2 + 5y^2 - 1 = 0$$
$$y = \sqrt{\frac{3x^2 + 1}{5}}$$



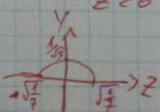
קריטר z=0 קריטר
השטח
המחולק

נאום מ x
-1 ו-1 הקוק
קריטר z

$$5y^2 + 7z^2 - 1 = 0$$

$$y = \sqrt{\frac{1 - 7z^2}{5}}$$

z=0 קריטר



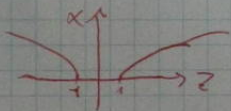
$$-\frac{1}{\sqrt{5}} \leq z \leq \frac{1}{\sqrt{5}}$$

$$z^2 \leq \frac{1}{7} \quad 7z^2 \leq 1 \quad \Leftrightarrow \frac{1 - 7z^2}{5} \geq 0$$

מאמ x
-1 ו-1 הקוק
קריטר z

$$-3x^2 + 7z^2 - 1 = 0$$

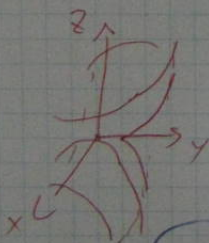
$$x = \sqrt{\frac{7z^2 - 1}{3}}$$



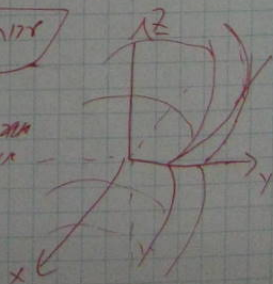
$$7z^2 - 1 \geq 0 \quad 7z^2 \geq 1 \quad z^2 \geq \frac{1}{7} \quad \boxed{z \geq \frac{1}{\sqrt{7}} \text{ או } z \leq -\frac{1}{\sqrt{7}}}$$

קריטר z = ± 1/√7 קריטר

קריטר z ≥ 1 או z ≤ -1
השטח המוקף



מאמ
מאמ קריטר
קריטר
מאמ קריטר
מאמ קריטר



-15

1. $\forall x \in \mathbb{R}, \exists y \in \mathbb{R} : x + y = 0$
 2. $\exists x \in \mathbb{R}, \forall y \in \mathbb{R} : x + y = 0$
 3. $\forall x \in \mathbb{R}, \forall y \in \mathbb{R} : x + y = 0$
 4. $\exists x \in \mathbb{R}, \exists y \in \mathbb{R} : x + y = 0$

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$$A = \begin{pmatrix} 1 & 0 & x \\ 0 & 0 & 0 \end{pmatrix} \begin{matrix} \begin{matrix} x-1=0 \\ x=0 \end{matrix} \\ \rightarrow \end{matrix}$$

~~$(x-1) = 0 \Rightarrow x = 1$~~

~~Handwritten scribbles and crossed-out text.~~

$$xI - A = \begin{pmatrix} x-1 & 0 \\ 0 & x \end{pmatrix} \det \Rightarrow (x-1)x = 0$$

$x=0, x=1$
 $\downarrow \quad \downarrow$
 1 1

(2)

$$|z+1+i| = |z+1-i|$$

$$(x+1+i(y+1))^2$$

$$|x+yi-1+i| = |x+yi+1-i|$$

$$(x+1)^2 + 2(x+1)i(y+1)$$

$$|x-1+i(y+1)| = |x+1+i(y-1)|$$

$$+ i^2(y+1)^2$$

$$x^2 + 2x + 1 + 2i(x+1)(y+1) - (y+i)^2$$

$$2i(xy+x+y+1)$$

$$x^2 + 2x + 1$$

$$x^2 + 2x + 1 + 2i(x+1)(y-1) - (y-i)^2$$

$$x^2 + 2x + 1 + 2i(xy+x+y+1) - y^2 + 2y - 1$$

$$x^2 - y^2 + 2(x-y) + 2i(xy+x+y+1)$$

$$(x+y)(x-y)$$

$$2i(x+1)(y-1) = |x+1|xy +$$

$$(x-y)(x+y+2) + 2i(x+1)(y-1)$$

$$|y-1| = |y+1|$$

$$y=0$$

$$x=0$$

$$x^2 + 2x + 1 + 2i(x+1)(y-1) - (y^2 - 2y + 1)$$

$$x^2 - y^2 + 2x + 2y + 2i(x+1)(y-1)$$

$$(x-y)(x+y) + 2(x+y)$$

$$|(x+y)(x-y+2) + 2i(x+1)(y-1)| = |(x-y)(x+y+2) + 2i(x+1)(y-1)|$$

$$|(x+y)(x-y+2)| = |(x-y)(x+y+2)|$$

$$|x^2 - y^2 + 2x + 2y| = |x^2 - y^2 + 2x - 2y|$$

$$|2y| = |-2y| \quad \underline{y=0}$$

שאלה מס' 4

א (15 נק') נתונים שני ישרים:

$$\frac{x}{5} = \frac{y}{6} = \frac{z-1}{8} \quad -1 \quad \begin{cases} 2x - 3y + z + 1 = 0 \\ 2x + y - 2z + 2 = 0 \end{cases}$$

מצאו משוואת המישור המכיל את שני הישרים (אם קיים).

~~4x - 2y - 2z = 0~~

5, 6, 8

~~4y = 3z - 1~~

5, 6, 3

~~2x - 6y =~~

6x - 5y + 4 = 0

$\frac{6x+4}{5} = y$

~~6x = 5y - 4~~

$\frac{6x+4}{5} = \frac{5y-4}{6} = \frac{3z-1}{-8}$

$\frac{x}{5} = \frac{6x+4}{5} \quad -\frac{5x+4}{5} = 0$

$\frac{y}{6} = \frac{5y-4}{6} \quad x = -\frac{4}{5}$

-4y = -4

y = 1

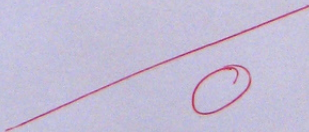
$-\frac{3z-1}{4} = \frac{2z-2}{4}$

3z = 3

z = 1

נק' מיוחד $(-\frac{4}{5}, 1, 1)$

כאשר \vec{r} הוא וקטור מיקום כלשהו של המישור
אז $\vec{r} \cdot \vec{n} = d$ כאשר \vec{n} הוא וקטור נורמלי למישור ו- d הוא המרחק מהמוצא למישור.



$$f(tx, ty) = f(x, y) \quad \text{I} \quad \text{II} \quad \text{③}$$

$$\frac{-t \quad \text{I} \quad \text{II} \quad \text{II} \quad \text{II}}{\text{II} \quad \text{II} \quad \text{II} \quad \text{II} \quad \text{II}}$$

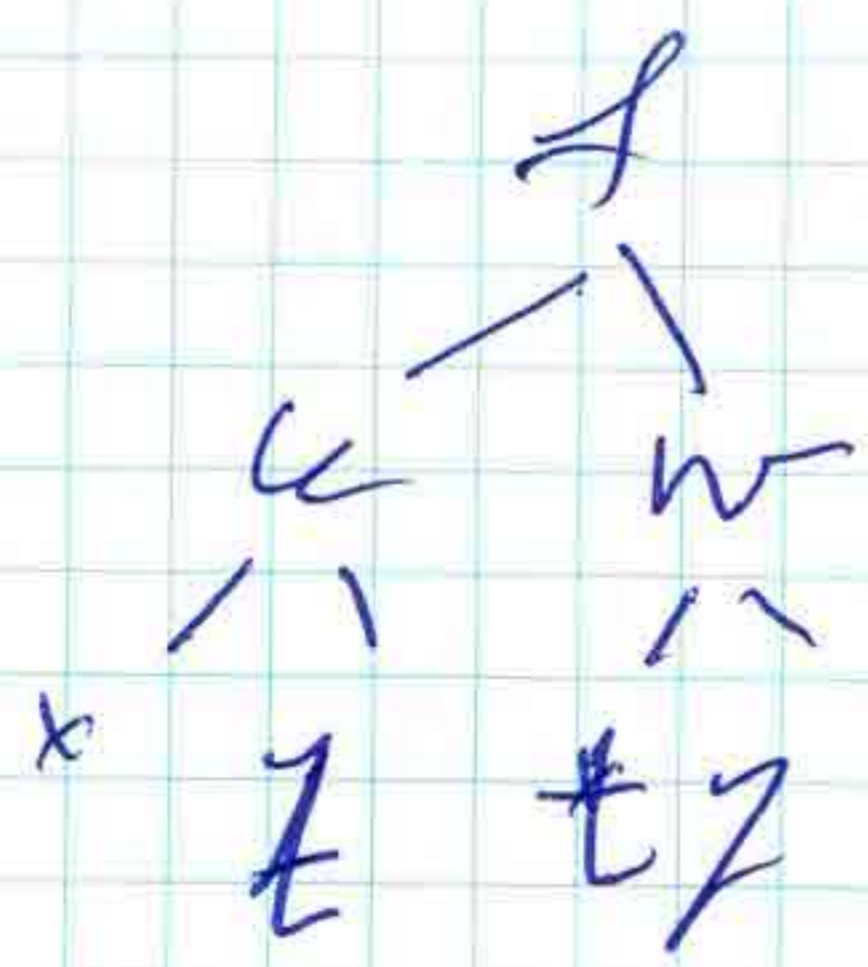
$$tx = \frac{x}{t} \quad \text{II} \quad \text{II} \quad \text{II} \quad \text{II} \quad \text{II}$$

$$ty = \frac{y}{t} \quad \text{II} \quad \text{II} \quad \text{II} \quad \text{II} \quad \text{II}$$

$$\text{I} \quad f_t = f_u \cdot u_t + f_w \cdot w_t$$

$$= f_u \cdot x + f_w \cdot y$$

→ x ו y



$$f_x = f_u \cdot u_x + f_w \cdot w_x =$$

$$f_x = f_u \cdot 1 + f_w \cdot 0 = f_u$$

$$\text{II} \quad \left(t^2 f(x, y) \right)'_t = 2t \cdot f(x, y) = f_u \cdot x + f_w \cdot y$$

$$\frac{\partial}{\partial t} (t^2 f(x, y)) = 2t f(x, y) \quad \left[t=1 \right]$$

$$2 f(x, y) = f_u \cdot x + f_w \cdot y$$

$$\frac{\partial f}{\partial x} \cdot x + \frac{\partial f}{\partial y} \cdot y$$

~~$f_x = f_x + f_w$~~

~~$f_{xx} = \frac{\partial f}{\partial t} + t \frac{\partial f}{\partial t}$~~

$$(2f_{x,y})'_x = \left(\frac{\partial f}{\partial t} \cdot x \right)'_x = \frac{\partial^2 f}{\partial (tx)^2} \cdot x + \frac{\partial f}{\partial tx} = f_{x,y}$$

$$(2f_{x,y})'_y = \left(\frac{\partial f}{\partial ty} \cdot y \right)'_y = \frac{\partial^2 f}{\partial (ty)^2} \cdot y + \frac{\partial f}{\partial ty} = f_{x,y}$$

$$2f_{x,y} = f_{tx} \cdot x + f_{ty} \cdot y = \frac{\partial f}{\partial tx} \cdot x + \frac{\partial f}{\partial ty} \cdot y$$

~~$\frac{\partial^2 f}{\partial (tx)^2}$~~

$2f_{x,y} = f_{xy} + f_{yx} =$

$$\left(\frac{\partial^2 f}{\partial (tx)^2} \cdot x + \frac{\partial f}{\partial tx} \right) \cdot x + \left(\frac{\partial^2 f}{\partial (ty)^2} \cdot y + \frac{\partial f}{\partial ty} \right) \cdot y$$

$$= \frac{\partial^2 f}{\partial tx^2} \cdot x^2 + 2 \frac{\partial^2 f}{\partial xy^2} \cdot x \cdot y + y^2 \cdot \frac{\partial^2 f}{\partial (ty)^2}$$

$f_{x,y} = f(x, ty) = t^{-1} f(x, y)$