Elementary Laplace Transforms

| $\boldsymbol{f}(\boldsymbol{t})=\boldsymbol{L}^{-1}\{\boldsymbol{F}(\boldsymbol{p})\}$ | $\boldsymbol{F}(\boldsymbol{p})=\boldsymbol{L}\{\boldsymbol{f}(\boldsymbol{t})\}$ |  |
| :---: | :---: | :---: |
| 1 | $\frac{1}{p}$ | $p>0$ (1) |
| $e^{a t}$ | $\frac{1}{p-a}$ | $\boldsymbol{p}>a$ |
| $\sin a t$ | $\frac{a}{p^{2}+a^{2}}$ | $\boldsymbol{p}>0$ (3) |
| cos at | $\frac{p}{p^{2}+a^{2}}$ | $\boldsymbol{p}>0$ (4) |
| $t^{n}, \quad n \in N$ | $\frac{n!}{p^{n+1}}$ | $\boldsymbol{p}>0$ |
| $t^{q}, \quad \boldsymbol{q}>-1$ | $\frac{\Gamma(q+1)}{p^{q+1}}$ | $\boldsymbol{p}>0$ (6) |
| $\sinh a t$ | $\frac{a}{p^{2}-a^{2}}$ | $p>\|a\|$ (7) |
| cosh at | $\frac{p}{p^{2}-a^{2}}$ | $p>\|a\|$ (8) |
| $e^{a t} \sin b t$ | $\frac{b}{(p-a)^{2}+b^{2}}$ | p>a (9) |
| $e^{a t} \cos b t$ | $\frac{p-a}{(p-a)^{2}+b^{2}}$ | $p>a(10)$ |
| $t^{n} e^{a t}, n \in N$ | $\frac{n!}{(p-a)^{n+1}}$ | $p>a(11)$ |
| $t \sin a t$ | $\frac{2 p a}{\left(p^{2}+a^{2}\right)^{2}}$ | $p>0$ (12) |
| $\boldsymbol{t c o s} \boldsymbol{a t}$ | $\frac{p^{2}-a^{2}}{\left(p^{2}+a^{2}\right)^{2}}$ | $p>0$ (13) |
| $\frac{\sin a t-a t \cos a t}{2 a^{3}}$ | $\frac{1}{\left(p^{2}+a^{2}\right)^{2}}$ | $p>0$ (14) |
| $\boldsymbol{u}_{\boldsymbol{c}}(\boldsymbol{t})$ | $\frac{e^{-c p}}{p}$ | $p>0$ (15) |
| $u_{c}(t) f(t-c)$ | $e^{-c p} F(p)$ | (16) |
| $\boldsymbol{e}^{c t} \boldsymbol{f}(\boldsymbol{t})$ | $\boldsymbol{F}(\boldsymbol{p}-\boldsymbol{c})$ | (17) |
| $\boldsymbol{f}(\boldsymbol{c t})$ | $\frac{1}{c} F\left(\frac{p}{c}\right)$ | $c>0$ (18) |
| $\int_{0}^{t} f_{1}(t-\tau) f_{2}(\tau) d \tau$ | $F_{1}(p) F_{2}(p)$ | (19) |
| $\delta(t-c)$ | $e^{-c p}$ | (20) |
| $(-\boldsymbol{t})^{\boldsymbol{n}} \boldsymbol{f}(\boldsymbol{t})$ | $F^{(n)}(\boldsymbol{p})$ | (21) |
| $f^{(n)}(t)$ | $p^{n} F(p)-p^{n-1} f(0)-\cdots-f^{(n-1)}(0)$ | (22) |

